Longevity 5:
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## POPULATION BASIS RISK AND HEDGE EFFECTIVENESS

## Hedging Longevity Risk

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# "Buy an annuity cheap, and make your life interesting to yourself and everybody else that watches the speculation." 

- Charles Dickens (1812-1870)


## Overview

■ Hedging longevity risk with index-based hedges
■ Can be beneficial because

- The only practical alternative for deferred pensions/annuities
- Some pension plans are too large to fully hedge any other way
- Cost and liquidity

■ Basis risk must be measured
■ Framework for basis risk analysis
■ Focus on Data and Context
■ Empirical analysis of UK and US case studies

- Widely available data

■ Evidence of stable relationships between them
■ Risk reduction using national population longevity index-based hedges can be significant if hedge optimally calibrated

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## What is basis risk?

- Basis risk refers to the mismatch associated with a hedging relationship
■ Present in most financial hedges
- Differences between underlying exposure and hedging instrument
- Leads to residual risks because the hedge is imperfect
- Longevity basis risk refers to mismatch in demographics between the beneficiaries of a pension plan or annuity portfolio and the population associated with the longevity hedging instrument
■ Gender basis
- Age basis
- Socioeconomic basis
- Geography basis


## Framework for analyzing basis risk and hedge effectiveness

$\square$ Framework must be aligned to the objective of longevity hedging
$\square$ Focus on the implications for hedge effectiveness
$\square$ Key elements:

1. Data:

- Metric
- Time horizon
- Analytical method

2. Context

- Framework must recognize that data is likely to be insufficient
$\square$ Most pension plans and annuity portfolios don't have enough historical data to draw rigorous statistical conclusions
$■$ Careful analysis using available data but also taking account of demographic, social and economic context


## Conclusions based on judgment not statistical proofs

## Metrics for analyzing basis risk

1. Mortality rates
2. Mortality improvements
3. Survival rates
4. Life expectancy
5. Liability cash flows
6. Liability values
-Simple comparison of mortality rates can be misleading $■$ Mortality rates do not directly relate to hedge effectiveness
■Annual mortality rates contain a lot of "noise"

## Time horizon for basis risk analysis should be long

- Longevity risk is a slowly-building cumulative trend risk that should be evaluated over long horizons
$\square$ Metrics should be compared over multi-year horizons
$\square$ This better reflects the nature of the risk
- Helps reduce the impact of noise that can give misleading results

■ But long horizons mean fewer independent observations available from historical data.

## Analytical methods

■ Analytical approaches to explore relationship between populations:

- Correlation
- E.g. correlation in improvements in mortality rates
- Regression
- E.g., regression of life expectancies through time

■ Graphical assessment

- E.g., stability of ratio of survival rates through time

■ Risk reduction

- E.g., reduction in volatility of liability value after hedging
- Techniques to reduce noise:

■ Graduation of mortality rates

- Age bucketing

■ Long-term horizon

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## UK males who own life assurance: "CMI Assured Lives"

- Assured population is an affluent subset of the national population

Data collected by the CMI (Continuous Mortality Investigation)

- Contributors are UK Life offices

Male assured lives (CMI)
■ Characterized by:

- Lower mortality rates

■ Higher mortality improvements

- Higher life expectancy
- Fewer lives at high agesNumber of lives variable
- Contributors vary


At face value basis risk relative to national population is "high"

## Setting the context

$\square$ CMI assured lives:

- A subpopulation of the UK national population
$\rightarrow$ Influenced by the same trends that impact national population
$\square$ Affluent, high income
$\rightarrow$ Lower mortality rates, higher life expectancy, faster improvements
- Data very noisy
$\rightarrow$ Changing contributors, changing numbers of lives and small numbers at high ages
- Implications
$\square$ The socioeconomic fabric of the UK means that mortality rates and life expectancies should not diverge without bound over the long run
- This doesn't mean that they converge, rather they shouldn't get too far apart over the long run
$\square$ Noise may mask underlying relationships, particularly at high ages


## Metric 1: Graduated mortality rates:

Assured lives vs. national population


Source: J.P. Morgan, LifeMetrics Index and CMI publications

Historical mortality rates age 65


Source: J.P. Morgan, LifeMetrics Index and CMI publications

At face value experience has been very different

## Comparing graduated mortality rates 1961-2005



## Assured population has lower mortality and higher improvements

## Metric 2: Mortality improvements converge over the long run

## Ratio of cumulative mortality improvements*: [assured / national]

## Age group 50-59



19621968197419801986199219982004
Source: J.P. Morgan, LifeMetrics Index and CMI publications

## Age group 70-79



Source: J.P. Morgan, LifeMetrics Index and CMI publications

## Age group 60-69



Source: J.P. Morgan, LifeMetrics Index and CMI publications

## Age group 80-89



Source: J.P. Morgan, LifeMetrics Index and CMI publications

* Ratio of annualized improvements since 1961


## Aggregate correlations of changes in mortality rates

Aggregate correlation for individual ages


Source: J.P. Morgan, LifeMetrics Index and CMI publications

Aggregate correlation for 10-yr age buckets


Source: J.P. Morgan, LifeMetrics Index and CMI publications

- Aggregate correlations between assured lives and national population
- Calculated as one correlation across time and age
- Graduated mortality rates, non-overlapping time periods
$\square$ Correlations increase with the time horizon
- But long horizons have few data points


## Metric 3: Survival rates historically have differed, but increased broadly in unison

## 10-yr survival rates for age 65



Source: J.P. Morgan, LifeMetrics Index and CMI publications

Ratio of 10-yr survival rates


Source: J.P. Morgan, LifeMetrics Index and CMI publications

- Ratio of survival rates [assured / national]
- Relatively constant through time
- Increases with age

■ 1.03 (age 45); 1.19 (age 65); 1.36 (age 75); 1.55 (age 80)

## Metric 4: Period life expectancy has increased broadly in step

Period life expectancy for age 65


Source: J.P. Morgan, LifeMetrics Index and CMI publications

Ratio of period life expectancy


Source: J.P. Morgan, LifeMetrics Index and CMI publications

- Ratio of life expectancy [assured / national]
- Relatively constant through time
- Increases with age

■ 1.14 (age 45); 1.22 (age 65); 1.24 (age 75); 1.24 (age 80)

## 45 -year change in period life expectancy has been approximately the same for all ages

## Increase of life expectancy 19612005 (years)



Source: J.P. Morgan, LifeMetrics Index and CMI publications

Increase of life expectancy 19612005 (\%)


Source: J.P. Morgan, LifeMetrics Index and CMI publications

■ Period life expectancy over 1961-2005

- Similar percentage increases between the two populations
- Greatest percentage increases for higher ages


## Metric 5: Liability cash flows realized over 10-year historical periods

Cumulative 10-yr cash flow age 65


Source: J.P. Morgan, LifeMetrics Index and CMI publications

## Ratio of 10-yr cash flow



Source: J.P. Morgan, LifeMetrics Index and CMI publications

- Lifetime annuity paying GBP1 annually to survivors of a cohort
- Calculate sum of cash flows over 10 years
$\square$ Ratio relatively constant through time
- Ratio increases with age


## Metric 6: Theoretical liability value: Fixed age perspective

## Liability value for age 65



Source: J.P. Morgan, LifeMetrics Index and CMI publications

## Ratio of liability values



- Lifetime annuity paying GBP1 annually to survivors of a cohort
$\square$ Calculate theoretical annuity price, using mortality projection model
- Ratio relatively constant through time
- Ratio increases with age

Note: The calibration look-back period for mortality projection is 30 years and discount rate is assumed to be $5 \%$

## Theoretical liability value: Cohort perspective

## Liability values for cohort aged 65 in 1991

## Ratio of liability values for different cohorts in 1991



Source: J.P. Morgan, LifeMetrics Index and CMI publications


Note: The calibration period for mortality projection is 30 years and discount rate is assumed to be $5 \%$

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## California vs US national population: males

- California population is a affluent subset of the national population

Data collected by same process for both

- Characterized by:
- Lower mortality rates
- Higher mortality improvements
- Higher life expectancy
- Large subpopulation
- Shorter history

| US vs Callifornia population statistics |  |  |  |
| :--- | :---: | :---: | :---: |
|  | National | California | $\%$ |
| Total (mm) | 304.1 | 36.8 | $12 \%$ |
| Over 65 (mm) | 38.9 | 4.1 | $11 \%$ |
| GDP per capita | $\$ 37,899$ | $\$ 42,064$ | $111 \%$ |

Source: U.S. Census Bureau and Bureau of Economic Analysis, 2008 figures

## Similar relationship to national population as in UK example, but closer match in terms of size and profile

## Metric 1: Graduated mortality rates:

California state population vs. US national population


Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

Historical mortality rates age 65


Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

## At face value experience looks comparable

## Comparing graduated mortality rates 1980-2004



Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

## Annualized improvements 1980-2004

Younger: 40-64 $\quad$ Older: 65-89


Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

## Metric 2: Mortality improvements converge over the long run

## Ratio of cumulative mortality improvements*: [California / national]

## Age group 50-59



Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

## Age group 70-79



Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

## Age group 60-69



Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

## Age group 80-89



Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

* Ratio of annualized improvements


## Aggregate correlations of changes in mortality rates

## Aggregate correlation for individual ages



Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications
Aggregate correlation for 10-yr age buckets


- Aggregate correlations between California and national population
- Calculated as one correlation across time and age
- Graduated mortality rates, non-overlapping time periods

Correlations increase with the time horizon
But long horizons have few data points
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## Metric 3: Survival rates historically increased broadly in unison

## 10-yr survival rates for age 65



Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

## Ratio of 10-yr survival rates



Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

■ Ratio of survival rates [California / national]

- Relatively constant through time
- Increases with age
- 1.00 (age 45); 1.04 (age 65); 1.07 (age 75); 1.09 (age 80)


## Metric 4: Period life expectancy has increased broadly in step

Period life expectancy for age 65


Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

Ratio of period life expectancy


Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

- Ratio of life expectancy [California / US national]

Relatively constant through time1.03(age 45); 1.05 (age 65); 1.05 (age 75); 1.05 (age 80)

## 25-year change in period life expectancy has been approximately the same for all ages



Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

## Increase of life expectancy 19802004 (\%)



Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

- Period life expectancy over 1980-2004
- Similar percentage increases between the two populations
- Greatest percentage increases for higher ages


## Metric 5: Liability cash flows realized over 10-year historical periods

Cumulative 10-yr cash flow age 65


Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

Ratio of 10-yr cash flow


Source: J.P. Morgan, LifeMetrics Index, U.S. Census Bureau and CDC publications

- Lifetime annuity paying \$1 annually to survivors of a cohort
- Calculate sum of cash flows over 10 years
- Ratio relatively constant through time
- Ratio increases with age

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## Conclusions from the US and UK examples

■UK Assured Lives

- Smallish subgroup of national population
- Noise in data

■ Age profile centered around people in their 40s, with few lives 65+

- Basis risk likely to be higher than for a large pension plan / annuity portfolio

■ California

- Large subgroup of national population
- Same process for data collection as national population, so less noise
$\square$ Both
- Affluent subpopulations, with lower mortality and higher life expectancy than respective national populations
- Have larger numbers of lives and longer history than typical insurer annuity portfolios or pension plans


## Implications for hedge effectiveness calculations:

Case study 1 - Retrospective effectiveness test (backtesting)

■ Case study: Longevity hedge based on national population index

- Hedge variability of cash flow
- Retrospective hedge effectiveness test

Hedge effectiveness for an index hedge: Historical case study


## Case Study2: Prospective hedge effectiveness test

■ Case study: Longevity hedge based on national population index

- Hedge variability of liability value

■ 94\% correlation between 10-year improvements for pension plan and LifeMetrics hedge

## Distribution of liability value in 10 years: Before and after hedging



## Summary

■ Framework for basis risk analysis:

- Focus on
- Data (metric, long horizon, analytical method)
- Context

■ Empirical analysis of UK and US case studies:
■ Significant evidence of stable relationships historically

- Correlations high when measured appropriately over long horizons
- Survivor rates, life expectancies, liability cash flows and value have moved proportionately over time
- Ratios are stable over the medium-to-long term

■ Risk reduction using national population longevity index-based hedges can be significant if hedge optimally calibrated

